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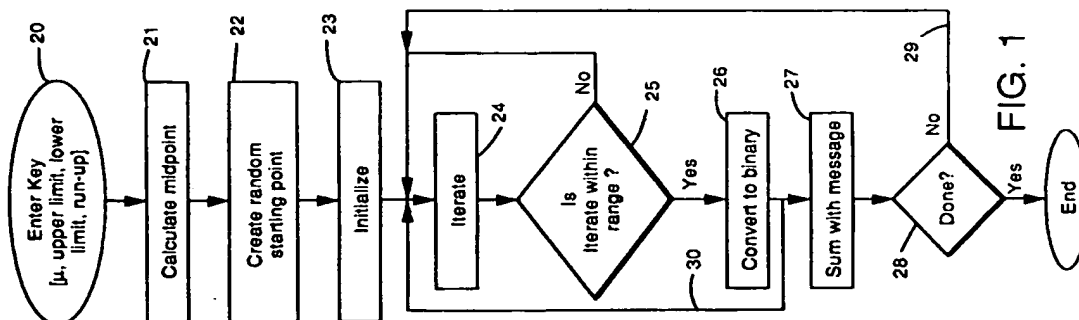
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54 An encryption system based on Chaos theory.

57 An encryption system and method based on the mathematics of Chaos theory, which provides protection of data from unauthorized modification and use during its storage and transmission. At its core are nonlinear equations which exhibits random, noise-like properties, given certain parameter values. When iterated, a periodic sequence is produced with an extremely long cycle length. A domain transformation process is then used to convert the floating-point iterates into binary form for summation with the digital data to be protected. The result is an encrypted message that cannot be modified, replaced, or understood by anyone other than the intended party. The use of Chaos theory in combination with the domain transformation process results in an easily implemented cryptographic system with extremely robust cryptographic properties. The concepts of the present invention also lend themselves well to either hardware or software implementations. The cryptographic system of the present invention may be employed to encrypt and decrypt sensitive information, to authenticate data and video links, or similar applications. It can also be used to provide a simple hash function for the secure storage of passwords in a computer system. Its simplicity, requiring only floating-point operations at its core, allows a lower cost and higher performance product with cryptographic security equivalent to conventional cryptographic systems.



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BACKGROUND

The present invention relates generally to encryption systems, and more particularly, to an encryption system that is implemented using the concepts of Chaos theory.

5 Cryptography is the science of protecting information from eavesdropping and interception. The two principle objectives are secrecy (to prevent unauthorized disclosure) and integrity (to prevent unauthorized modification). A number of products are available to provide this protection, but they tend to be complex and slow, or fast but cryptographically not very robust. The Data Encryption Standard (DES) is one example of a robust algorithm, however its software implementations are slow due to its complexity, and its hardware
10 implementations require complex devices. Proprietary algorithms have also been used, however their strength is not always verifiable since design details are usually not publicly disclosed. In addition, complex algorithms require significant human and computing resources to prove their strength, and even then hidden weaknesses are occasionally discovered at a later time. The present invention overcomes these problems.

The DES and Rivest Shamir Aldeman (RSA) cryptographic systems are the best known and most
15 widely used products available for comparison. The Data Encryption Standard and the present invention perform similar functions and can generally be used in the same applications. The DES is available in either hardware or software versions, allowing flexibility for the application developer. The disadvantage with software versions of the DES is that its algorithm is based on a complex state machine, and state machines do not translate well into software. Computers are much better suited to operations on 8-, 16-, or 32-bit
20 words, and DES requires intensive operations at the individual bit level. One DES implementation that was tested required the execution of about 5,000 high-level software statements, which is unnecessarily high.

The RSA algorithm can likewise be implemented in software or hardware, although hardware is the most common, since its processes rely on complicated mathematics which execute too slowly in software for most applications. In addition to its slow speed, another disadvantage is that while being considered
25 computationally secure today, it may not be in the future. Its strength is based on the computationally difficult problem of factoring large prime numbers. If a more efficient algorithm were to be discovered, its security could be weakened. Since this invention cannot be reduced to such a simple mathematical function, it represents a more robust system. The present invention overcomes the problems associated with the Data Encryption Standard and RSA cryptographic systems.

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SUMMARY OF THE INVENTION

This invention is an encryption system based on the mathematics of Chaos theory, which provides protection of data from unauthorized modification and use during its storage and transmission. At its core is
35 a nonlinear equation which exhibits random, noise-like properties when certain parameters are used. In particular, one such nonlinear equation is the logistic difference equation: $x_{n+1} = \mu x_n(1-x_n)$, which is chaotic for certain values of μ , wherein μ acts as a tuning parameter for the equation. When iterated, a periodic sequence is produced with an extremely long cycle length. A domain transformation process is then used to convert the floating-point iterates into binary form for summation with the digital data to be protected. The
40 result is an encrypted message which cannot be modified, replaced, or understood by anyone other than the intended party. The use of Chaos theory in combination with the domain transformation process results in a cryptographic system with extremely robust cryptographic properties.

A simple mathematical formula with complex properties is used instead of a complex state machine with complex properties. This allows faster operation, while at the same time reduces the possibility of a
45 hidden or undiscovered cryptographic weakness. In addition, knowledge of the algorithm does not simplify recovery of the key. In fact, even when the conditions most favorable to a cryptanalyst are allowed, key protection is maintained when other more conventional systems would be broken. This is made possible by a unique one-way domain transformation process which results in the loss of information critical to the cryptanalyst's success. The combination of these techniques results in a cryptographic system that is
50 extremely simple to implement, yet is cryptographically very robust. It also lends itself well to either a hardware or software implementation.

The cryptographic system of the present invention may be employed to protect sensitive information, or to authenticate data and video links, or to support secure computer systems, or similar applications. It can also be used to provide a simple hash function for the secure storage of passwords in a computer system.
55 Its simplicity, requiring only floating-point operations at its core, allows a lower cost and higher performance product with cryptographic security equivalent to the most widely used cryptographic systems.

BRIEF DESCRIPTION OF THE DRAWINGS

The various features and advantages of the present invention may be more readily understood with reference to the following detailed description taken in conjunction with the accompanying drawings, wherein like reference numerals designate like structural elements, and in which:

- 5 FIG. 1 is a flowchart showing an encryption process in accordance with the principles of the present invention;
- FIG. 2 is a flowchart showing a decryption process in accordance with the principles of the present invention;
- FIG. 3 is a diagram showing an encryption and decryption system without error extension in accordance with the principles of the present invention;
- 10 FIG. 4 is a diagram showing an encryption and decryption system with error extension in accordance with the principles of the present invention; and
- FIG. 5 is a functional block diagram of the encryption and decryption system in accordance with the principles of the present invention.

15 DETAILED DESCRIPTION

By way of introduction, Chaos theory is an evolving field of mathematics that studies the behavior of nonlinear systems. When properly initialized, these systems exhibit chaotic behavior when iterated. Chaotic behavior may be described as a form of steady state behavior which is aperiodic and as such appears to have noise-like characteristics. This behavior, although aperiodic, is bounded, and while the chaotic trajectory never exactly repeats itself, the trajectory is completely deterministic given the exact initial conditions and parameter values. These chaotic properties are used to generate an aperiodic sequence for use as the keystream in the encryption system of the present invention.

It is useful to draw an analogy with a common linear sequence generator. Both the present invention and the linear sequence generator produce pseudo-random sequences from a given starting point, and both have a finite cycle length. However, the frequency spectrum of a chaotic system is continuous and broadband, whereas the linear sequence generator is discrete. This property offers significant advantages when used in an encryption system, since its statistical properties are more noise-like when small sections of the entire state space are considered. For example, the statistical performance of a 1,000 bit sample taken from a linear sequence generator with 10 million states will not appear very noise-like due to the small percentage of available states used. A chaotic system under the same conditions would appear more noise-like.

The logistic difference equation is one of the simplest nonlinear functions which exhibits chaotic characteristics, and is the first of two processes used in the present invention. Although this function is used in the following description, it is only one of a number of functions with similar properties. The concepts of the present invention permit any of this entire class of functions to be used. The logistic difference equation is defined as: $x_{n+1} = \mu x_n(1-x_n)$, where μ is a constant between 0.0 and 4.0 and x is the iterated result between 0.0 and 1.0. Approximately 90% of μ values between 3.57 and 4.0 result in chaotic behavior, and the particular value selected remains constant throughout the iterations. An initial value of x_n is chosen to begin the process. An extremely minor change to this initial value will result in a completely different sequence; 0.1000000000 will produce a different sequence than 0.1000000001. The initial values simply determine different starting positions in the same very long sequence for any given value of μ .

It has been mathematically proven that operation in the chaotic region will produce an aperiodic sequence, making it appear as if an infinite cycle length can be obtained. Reference is hereby made to the thesis by Dana Reed entitled "Spectrum Spreading Codes from the Logistic Difference Equation," submitted to the Department of Electrical Engineering and Computer Science at the University of Colorado, having a reference number of LD1190.E54 1989M R43, the contents of which are incorporated herein by reference.

In practice, however, the floating-point precision of the machine implementation determines the maximum cycle length that is available. With the 12-digit precision typically available on most computers, the maximum cycle length would be on the order of 10^{12} iterates. An IBM-PC with a math coprocessor could produce about 10^{19} iterates. Due to the number of variable parameters, however, it is extremely difficult to determine an exact cycle length. This has both advantages and disadvantages for an encryption application. For comparison, the Data Encryption Standard has a cycle length of about 10^{16} states. To illustrate the magnitude of these numbers, a system implementing this algorithm and operated continuously at a 1 Megabit/sec rate would not repeat for 11.6 days with 10^{12} iterates, and for 317,000 years with 10^{19} iterates. Given the same conditions, the Data Encryption Standard would not repeat for 317 years. This illustrates the flexibility of the present invention, since extremely long cycle lengths can be obtained by

simply increasing the precision of the implementation.

Two characteristics of the above logistic difference equation allow it to be used within an encryption system. First, for any given μ and x_n , the logistic difference equation deterministically generates an extremely large number of uniformly distributed iterates. This allows a decryptor to easily obtain synchro-
 5 nization with the encryptor, and the uniform statistical distribution increases the robustness of the encrypted data against recovery by cryptanalysis. Second, changing the value of μ or x will result in a totally different sequence, allowing μ to be used as the "key" and x_n as the "preamble".

The second function used in the present invention is a domain transformation process. Since the logistic difference equation produces real numbers between 0.0 and 1.0, its iterates must be converted to a
 10 binary 0 or 1 before encryption of digital data can take place. This is accomplished with a two-stage numerical filter process. The first stage limits the range of iterate values to be used and the second stage converts them into a binary 0 or 1. Iterates between the lower limit and midrange are converted into 0's, and iterates between the midrange and upper limit are converted into 1's. This is essentially a transformation from the continuous domain to the discrete domain, which is an irreversible process.

This transformation results in significantly greater cryptographic strength than use of the logistic difference equation alone. For example, by passing only those values between 0.4 and 0.6 to the second stage, a significant number of intermediate iterates will never become part of the keystream. Due to the irreversible nature of this transformation and the use of a discontinuous number of iterates, the actual x_n values cannot be recovered from knowledge of the binary keystream. By denying a cryptanalyst of this
 20 information, the work factor required to recover the message or its key from the transmitted data increases to the point of computational infeasibility. The number of variables involved also allow the iterates to be periodically perturbed, effectively adding another discontinuity to further complicate cryptanalysis.

Due to the nature of the present invention, a software implementation thereof is a natural choice. Any computer capable of floating-point operations can be used. The optional use of a math coprocessor offers
 25 the benefit of increased execution speed, and its higher precision increases the effective state space. Flowcharts of the encryption and decryption processes, and a system diagram of a typical implementation are shown in FIGS. 1, 2, and 3, respectively, and an implementation in the Pascal language is provided in Appendix I hereto.

With reference to FIG. 1, which illustrates the encryption sequence of the present invention, the
 30 parameter μ , the upper and lower limits of the iterate range, and an initialization count (run-up) are supplied as the "cryptographic key" in step 20. The midpoint between the upper and lower limits is then calculated in step 21 for later use by the domain transformation process. A random starting point is then created in step 22 which is nonrepeatable and nonpredictable between encryption sessions. This will be the initial value of x_n , and is saved so that it can be prepended to the following encrypted message. Examples are the
 35 time and date when encryption is initiated, or a variety of system-specific parameters previously agreed upon by the encryptor and decryptor. The equation is then iterated in step 23 for the run-up amount specified in the key to determine the initial starting point. The next iterate is then generated in step 24 and tested in step 25 to determine if it is within the specified range. If so, it is converted into a binary 0 or 1 in step 26, otherwise it is ignored and a new iterate is calculated and tested by repeating steps 24 and 25.
 40 The resulting binary value is summed modulo-2 in step 27 with one bit of plain text (data to be encrypted), creating a ciphertext bit which can either be stored or immediately output. This process is repeated until the entire message has been encrypted as indicated by the decision block 28 and loop 29. Although this description performs encryption on a bit-for-bit basis, multiple-bit words may also be encrypted by repeating steps 24, 25, and 26 an appropriate number of times before summing with a multiple-bit block of
 45 the message. This is illustrated by loop 30 in FIG. 1. For example, an 8-bit byte may be encrypted by generating 8 bits of keystream, then performing step 27 only once.

The decryption process is similar. With reference to FIG. 2, the cryptographic key is loaded in step 40 and the midpoint is calculated in step 41. Using encryptor randomization based on the time and date, for example, the initial value of x_n will be received with the encrypted message as indicated in step 42. Using
 50 system-specific parameters, the initial value may either be transmitted with the message or calculated independently by the receiver according to the agreed upon procedure. As before, the equation is initialized and iterated the proper number of times as indicated by steps 43, 44, and 45, followed by generation of the keystream by converting the iterates to binary, as shown in step 46. When modulo-2 summed with the ciphertext in step 47, the original message is recovered. The multiple-bit word decryption steps are
 55 illustrated by loop 50 which corresponds to loop 30 in FIG. 1.

A typical software implementation is provided in Appendix I hereto. The same procedure may be used for encryption and decryption, depending on whether the plain message or ciphertext is used for "data".

FIG. 3 illustrates an implementation of an encryption and decryption system 60. The system 60 uses a

cryptographic key 61 and a randomly created initial value 62 within a keystream generator 63 comprised of the logistic difference equation and domain transformation process. The output of the process 63 is coupled to a modulo-2 adder 64 that combines the message to be encrypted with a binary value generated by the keystream generator 63 to produce encrypted ciphertext. The ciphertext is then communicated to the decryption portion of the system 60. The cryptographic key 65 and received initial value 66 are used by a
 5 keystream generator 67 comprising the logistic difference equation and domain transformation process. The output of the keystream generator 67 is coupled to a modulo-2 adder 68 that combines the message to be decrypted with the binary value generated by the keystream generator 67 to recover the original message.

The above-described system 60 and methods have no error extension, so that a single bit error in the
 10 received ciphertext results in one incorrect bit in the decrypted message. A minor modification to the system 60 and its processes, however, provide an error extending mode of operation. A diagram of this modified system 60a is shown in FIG. 4. Keystream bits are fed sequentially into a first-in-first-out array 72 by way of a modulo-2 adder 71, instead of being immediately used. As each bit of the message is encrypted, the ciphertext is modulo-2 added with a new keystream bit and fed back into the array. After a
 15 short delay, it is then modulo-2 summed again with another bit of the message. Similarly, the decryption portion of the system 60a also includes an additional adder 74 and a FIFO array 75, which operate as described above. In this case, a single bit error in the received ciphertext will result in a number of errors as it propagates through the array. For example, a 4-element array produces 16 errors for each ciphertext bit. Assuming that the following ciphertext is received error-free, recovery of the original message then
 20 continues.

Implementing the above-described algorithm in hardware offers the benefits of increased speed and greater protection against reverse engineering and unauthorized modification. Any hardware implementation may be used, including off-the-shelf microprocessors and digital signal processors, gate arrays, program-
 25 mable logic devices, or full custom integrated circuits. For descriptive purposes, only the gate array option is discussed below. It performs all of the functions previously discussed, and its arithmetic logic unit may be customized in a conventional manner to provide the desired level of floating point precision. A functional block diagram of the hardware system 80 is shown in FIG. 5. At its core is an arithmetic logic unit 81 capable of floating point operations to the precision desired. An arithmetic logic unit controller 82 implements the necessary control logic in a conventional manner to iterate a variety of predefined chaotic
 30 equations, and provides the numerical filter and binary conversion functions. Since the arithmetic logic unit 81 needs to produce many iterates for each keystream bit when narrow filters are used, a separate system clock at an operating frequency greater than the data clock is provided to maintain high encryption rates. The remaining portions of the system 80 provide support functions, and include a randomizer 83, key storage memory 84, an I/O interface 85, a control sequencer 86 and a modulo-2 adder 87. However, it is the
 35 arithmetic logic unit 81 and arithmetic logic unit controller 82 which implement the functions performed by the present invention. The I/O interface 85 communicates with a host processor (not shown), and the control sequencer 86 directs the overall operations of the system 80. The key storage memory 84 is provided to store multiple keys, and the randomizer 83 provides random number generation for algorithm initialization.

The same system 80 may be used for both encryption and decryption since the process is symmetric.
 40 As mentioned above, I/O configurations and the randomization process are not specified herein since they are specific to each particular host system. Although the algorithm is best suited to processing serial data, a parallel architecture may be implemented by including the appropriate serial-to-parallel converters.

A software program embodying this invention was developed to investigate its properties. All critical functions and processes claimed herein were implemented, and encryption and decryption of sample
 45 messages were successfully demonstrated. In addition, a variety of standard statistical tests were performed on samples of 1 million keystream bits, using many combinations of the variable parameters. Tables 1 and 2 illustrate the distributions of typical 1 million bit samples. They indicate that the keystreams were statistically unbiased, and that totally different keystreams were obtained from minor changes to the initial conditions. Auto-correlation and cross-correlation tests were also performed, which confirmed that the
 50 keystreams were indeed nondeterministic. For comparison, Table 3 illustrates the performance of a standard Department of Defense (DoD) randomizer that uses a random physical process as its noise source. It is clear that the performance of the present invention compares favorably. This randomness is an essential property of all cryptographically robust encryption systems.

Table 1

$$\mu = 3.9996, \sigma = 0.1, \chi^2 = 216.2$$

lower limit = 0.49, upper limit = 0.51

Mono bit = 0.5000 First Delta = 0.4998 Second Delta = 0.4999 Third Delta = 0.5003

	0:	1:	2:	3:	4:	5:	6:	7:	8:	9:	A:	B:	C:	D:	E:	F:
0:	509	479	472	476	460	467	518	480	496	498	467	507	512	501	501	446
10:	508	475	508	499	488	465	487	501	493	495	496	486	461	532	487	452
20:	488	500	465	489	499	454	488	475	496	501	505	467	495	497	505	456
30:	478	473	456	476	481	534	513	488	489	476	505	509	499	476	520	478
40:	509	480	505	488	487	500	458	478	484	483	442	464	507	519	479	540
50:	476	484	484	461	481	514	470	462	455	477	482	450	472	470	471	492
60:	475	502	480	495	490	521	456	501	475	465	519	475	462	515	500	465
70:	504	508	493	489	466	502	499	503	515	487	468	525	512	496	502	442
80:	486	505	484	548	500	459	515	465	491	487	488	468	476	467	502	499
90:	495	484	475	501	483	506	500	492	489	480	502	475	486	488	520	496
A0:	480	477	482	479	489	446	534	450	491	490	518	494	512	459	470	482
B0:	466	495	495	487	490	529	504	472	513	493	504	500	463	486	504	481
C0:	510	457	489	515	456	510	484	481	525	520	500	502	502	477	481	495
D0:	504	522	460	491	478	514	488	488	465	480	497	522	516	511	477	468
E0:	478	464	467	460	485	467	507	484	522	487	470	497	424	498	498	496
F0:	518	443	456	476	500	494	460	511	486	489	482	509	464	521	492	479

Run Count	Zeros	Ones	Expected Value
1	125382	124729	125000
2	62384	62754	62500
3	30993	31526	31250
4	15682	15537	15625
5	7798	7900	7812
6	3963	3792	3906
7	1888	1919	1953
8	987	953	976
9	468	508	488
10	279	250	244
11	124	110	122
12	74	58	61
>12	70	56	61

Table 2

$$\mu = 3.9996, x = 0.1000000001, \chi^2 = 245.9$$

$$\text{lower limit} = 0.49, \text{upper limit} = 0.51$$

Mono bit = 0.5000 First Delta = 0.4999 Second Delta = 0.4998 Third Delta = 0.4997

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	0:	1:	2:	3:	4:	5:	6:	7:	8:	9:	A:	B:	C:	D:	E:	F:
0:	510	476	495	488	502	474	513	505	475	486	479	488	466	503	500	520
10:	489	500	468	507	510	471	454	490	448	494	531	462	511	495	476	503
20:	479	519	503	484	491	499	479	508	474	527	520	484	478	487	522	478
30:	510	504	508	470	479	477	461	443	522	472	422	471	473	474	498	488
40:	486	493	530	484	494	468	470	469	484	467	525	531	464	476	445	499
50:	495	466	482	516	495	503	455	494	488	492	479	506	493	508	500	529
60:	460	492	517	484	516	476	526	529	506	465	483	493	500	453	514	488
70:	478	538	509	474	470	501	505	487	457	478	490	472	510	501	455	496
80:	487	455	457	502	508	504	491	477	498	501	466	466	490	517	491	462
90:	501	485	448	514	472	508	497	474	478	472	500	506	444	469	484	485
A0:	495	484	436	494	489	498	506	527	467	441	496	469	494	448	459	495
B0:	480	492	519	527	468	514	476	491	482	484	513	508	492	527	528	466
C0:	487	496	483	503	484	470	490	510	489	468	467	510	487	494	530	476
D0:	488	477	465	497	471	486	451	447	488	494	497	423	507	492	486	501
E0:	488	473	458	534	491	502	468	462	513	456	521	505	476	528	538	457
F0:	457	426	487	491	495	482	467	506	496	491	497	466	456	487	480	491

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Run Count	Zeros	Ones	Expected Value
1	125217	124825	125000
2	62411	62582	62500
3	31137	31624	31250
4	15725	15312	15625
5	7718	8016	7812
6	3955	3872	3906
7	1920	1914	1953
8	1016	965	976
9	444	480	488
10	269	245	244
11	118	93	122
12	65	72	61
>12	67	62	61

55

Table 3

The output from a DoD approved random source. $\chi^2 = 283.2$

Mono bit = 0.4994 First Delta = 0.5001 Second Delta = 0.5002 Third Delta = 0.4997

	0:	1:	2:	3:	4:	5:	6:	7:	8:	9:	A:	B:	C:	D:	E:	F:
0:	514	433	497	502	488	545	508	505	498	485	502	470	505	512	495	505
10:	528	526	469	516	502	468	499	459	466	517	497	492	479	510	464	508
20:	516	511	508	471	486	496	474	453	473	486	516	482	481	528	484	489
30:	508	465	478	493	482	479	510	481	522	488	484	483	510	484	466	481
40:	463	444	474	509	495	472	484	504	510	486	461	484	510	473	493	467
50:	473	487	473	440	529	518	529	460	500	516	498	507	452	506	534	482
60:	453	485	490	515	460	496	426	505	492	498	477	483	463	550	443	479
70:	503	496	485	462	462	535	490	478	475	462	455	515	517	483	504	475
80:	485	507	520	480	499	490	487	461	465	467	449	478	460	500	509	478
90:	488	470	445	445	457	481	511	466	485	468	517	491	469	464	471	461
A0:	483	472	450	511	497	476	498	493	519	473	497	501	500	482	520	532
B0:	529	492	499	511	458	474	465	521	504	463	512	491	451	451	441	488
C0:	488	482	498	486	451	468	539	491	525	472	498	521	468	497	478	488
D0:	537	495	538	510	509	484	510	492	523	499	479	481	464	458	474	496
E0:	482	472	474	502	488	469	499	510	504	489	504	463	466	450	498	510
F0:	494	475	479	500	497	425	517	488	486	484	458	513	510	529	473	438

Run Count	Zeros	Ones	Expected Value
1	125202	124815	125000
2	61970	62780	62500
3	31213	31416	31250
4	15720	15366	15625
5	7880	7767	7812
6	4062	3918	3906
7	1946	1951	1953
8	996	998	976
9	492	505	488
10	234	218	244
11	115	99	122
12	49	65	61
>12	70	52	61

Thus there has been described a new and improved encryption system that is implemented using the concepts of Chaos theory. It is to be understood that the above-described embodiments are merely illustrative of some of the many specific embodiments which represent applications of the principles of the present invention. Clearly, numerous and other arrangements can be readily devised by those skilled in the art without departing from the scope of the invention.

APPENDIX I

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	<u>Code</u>	<u>Comments</u>
	BEGIN	
10	get_key;	{key contains fields for μ , {upper_limit, lower_limit, run-up,
	midpoint: = (upper_limit + lower_limit)/2	{calculate midpoint
15	randomize;	{call a routine to generate a random {starting point
	x: = random_value;	{assign random value as the initial value
	for temp = 0 to run_up	{initialize by iterating for the amount {specified by run-up
20		
	x: = $\mu * x - \mu * x * x$;	
	repeat	{repeat for entire message
25	repeat	{iterate until x is between lower and {upper limits
	x: = $\mu * x - \mu * x * x$;	
30	until (x > lower_limit) and (x < upper_limit)	
	if x > midpoint then keystream : = 1	{convert to binary
	else keystream : = 0;	
35	output : = keystream XOR data;	{encrypt
	until end of message;	{done
	END	

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Claims

1. A method of encrypting data comprising the steps of:
generating a random value having a selected mathematical precision;
45 generating an initial state of a predetermined chaotic equation by iterating with the random value
and a key value having a selected mathematical precision, for a selected number of iterations;
iterating the chaotic equation to generate a periodic sequence of encrypting iterates having an
extremely long cycle length;
performing a domain transformation by converting the encrypting iterates into binary form; and
50 summing the encrypting iterates in binary form with digital data to be encrypted to generate
encrypted data.
2. The method of Claim 1 wherein the step of iterating the chaotic equation further comprises the step of:
reiterating the the chaotic equation to generate a periodic sequence of encrypting iterates whose
55 values are within a selected range.
3. The method of Claim 1 wherein the predetermined chaotic equation comprises the logistic difference
equation $x_{n+1} = \mu x_n(1-x_n)$, where μ is a constant and x is an iterated result.

4. The method of Claim 1 wherein the step of iterating the chaotic equation further comprises selecting a desired mathematical precision for the iterating process to alter the periodic sequence of encrypting iterates.
- 5 5. The method of Claim 1 wherein the step of iterating the chaotic equation comprises the step of iterating the chaotic equation using a discontinuous set of encrypting iterates.
6. The method of Claim 1 wherein the step of iterating the chaotic equation comprises the step of periodically perturbing the iterates to add a further discontinuity in the binary encrypting iterates generated by the domain transformation step.
- 10 7. The method of Claim 1 wherein the step of iterating the chaotic equation further comprises the steps of:
feeding back the encrypted data;
summing the encrypted data with the periodic sequence of encrypting iterates to generate a
15 second set of encrypting iterates;
delaying the summed second set of encrypting iterates for a selected time period; and
summing the delayed second set of encrypting iterates with digital data to be encrypted to generate encrypted data.
- 20 8. The method of Claim 1 further comprising the steps of:
iterating the chaotic equation and performing the domain transformation a selected number of times; and
then summing the encrypting iterates with digital data to be encrypted to generate encrypted data.
- 25 9. A method of decrypting data encrypted in accordance with the method of Claim 1, said method comprising the steps of:
receiving encrypted data that is to be decrypted;
receiving the random value.
generating an initial state of the chaotic equation by iterating with the random value and a key
30 value, for the selected number of iterations;
iterating the chaotic equation to generate a periodic sequence of decrypting iterates having an extremely long cycle length;
performing a domain transformation by converting the decrypting iterates into binary form; and
summing the decrypting iterates in binary form with the encrypted digital data to be decrypted to
35 generate decrypted data.
10. The method of Claim 9 wherein the step of iterating the chaotic equation further comprises the step of:
reiterating the the chaotic equation to generate a periodic sequence of decrypting iterates whose
40 values are within a selected range.
11. The method of Claim 9 wherein the predetermined chaotic equation comprises the logistic difference equation $x_{n+1} = \mu x_n(1-x_n)$, where μ is a constant and x is an iterated result.
12. The method of Claim 9 wherein the step of iterating the chaotic equation further comprises the steps of:
45 summing the encrypted data with the periodic sequence of decrypting iterates in binary form to generate a second set of decrypting iterates;
delaying the second set of decrypting iterates for a selected time period; and
summing the delayed second set of decrypting iterates with encrypted data to be decrypted to generate decrypted data.
- 50 13. The method of Claim 9 further comprising the steps of:
iterating the chaotic equation and performing the domain transformation a selected number of times; and
then summing the decrypted iterates with encrypted data to generate decrypted data.
- 55 14. A method of encrypting data comprising the steps of:
generating a random value having a selected mathematical precision;
generating an initial state of a predetermined logistic difference equation by iterating with the

random value and a key value having a selected mathematical precision, for a selected number of iterations;

iterating the logistic difference equation to generate a periodic sequence of encrypting iterates having an extremely long cycle length;

- 5 performing a domain transformation by converting the encrypting iterates into binary form; and
summing the encrypting iterates in binary form with digital data to be encrypted to generate encrypted data.

- 15 15. The method of Claim 14 wherein the step of iterating the logistic difference equation further comprises the step of:
reiterating the the chaotic equation to generate a periodic sequence of encrypting iterates whose values are within a selected range.

16. The method of Claim 14 wherein the logistic difference equation comprises the equation $x_{n+1} = \mu x_n(1 - x_n)$, where μ is a constant and x is an iterated result.

17. The method of Claim 14 wherein the step of iterating the logistic difference equation further comprises adjusting the mathematical precision of the random value and key value to adjust the cycle length of the periodic sequence of encrypting iterates.

- 20 18. The method of Claim 14 wherein the step of iterating the logistic difference equation comprises the step of iterating the logistic difference equation using a discontinuous set of encrypting iterates.

- 25 19. The method of Claim 14 wherein the step of iterating the logistic difference equation comprises the step of periodically perturbing the iterates to add a further discontinuity in the binary encrypting iterates generated by the domain transformation step.

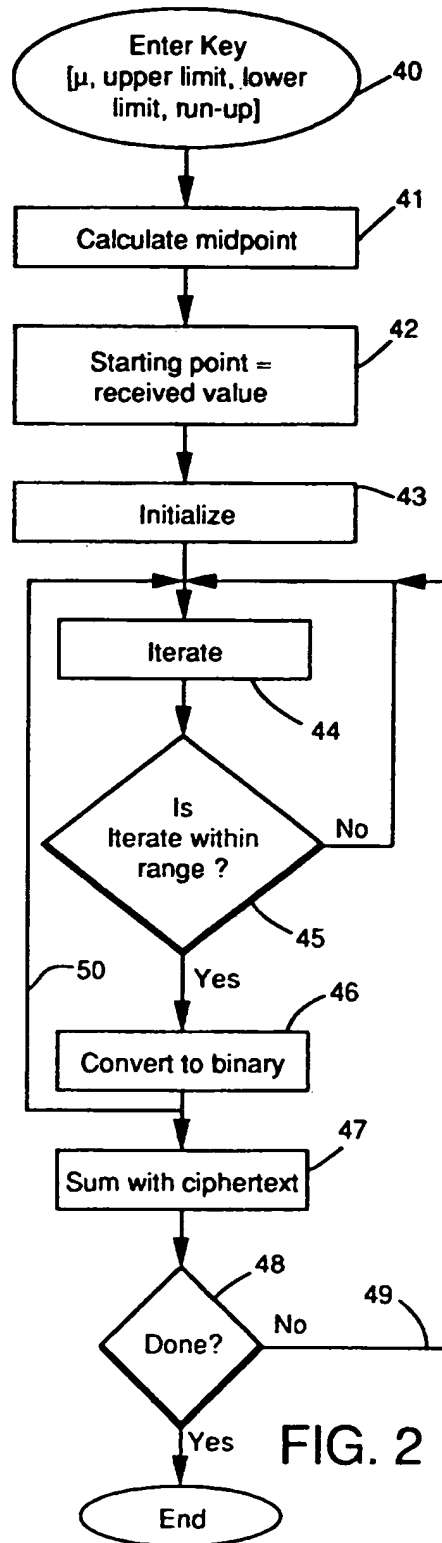
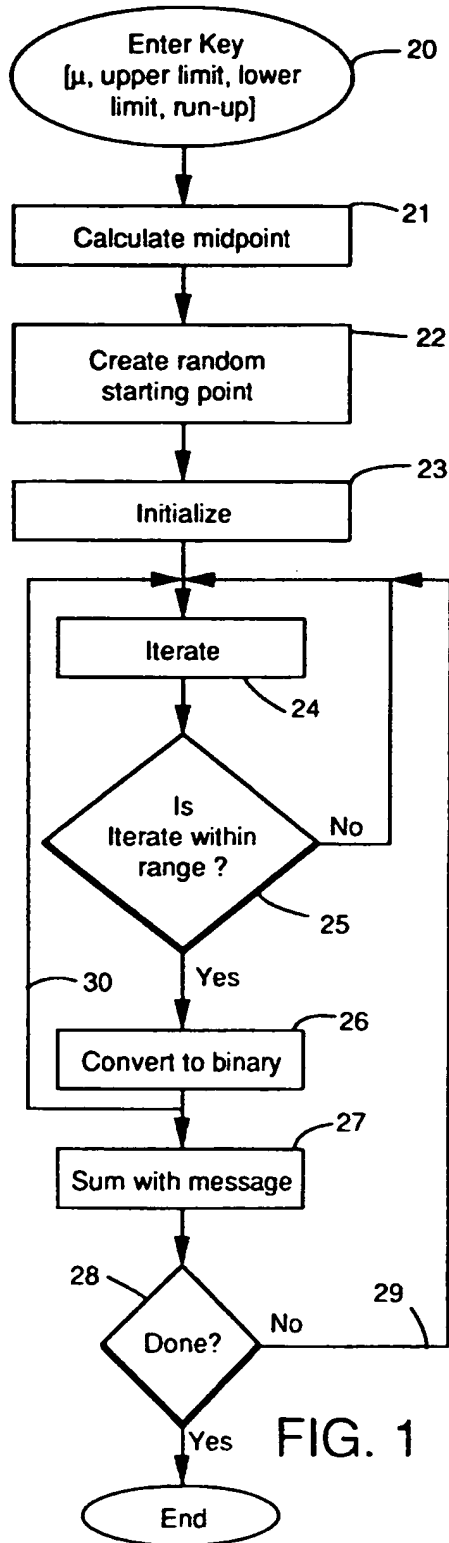
20. The method of Claim 14 wherein the step of iterating the logistic difference equation further comprises the steps of:
30 feeding back the encrypted data;
summing the encrypted data with the periodic sequence of encrypting iterates to generate a second set of encrypting iterates;
delaying the summed second set of encrypting iterates for a selected time period;
35 summing the delayed second set of encrypting iterates with digital data to be encrypted to generate encrypted data.

21. The method of Claim 14 further comprising the steps of:
iterating the logistic difference equation and performing the domain transformation a selected number of times; and
40 then summing the encrypting iterates with digital data to be encrypted to generate encrypted data.

22. A method of decrypting data encrypted in accordance with the method of Claim 14, said method comprising the steps of:
receiving encrypted data that is to be decrypted;
45 receiving the random value.
generating an initial state of the logistic difference equation by iterating with the random value and a key value, for the selected number of iterations;
iterating the logistic difference equation to generate a periodic sequence of decrypting iterates having an extremely long cycle length;
50 performing a domain transformation by converting the decrypting iterates into binary form; and
summing the decrypting iterates in binary form with the encrypted digital data to be decrypted to generate decrypted data.

23. The method of Claim 22 wherein the step of iterating the logistic difference equation further comprises the step of:
55 reiterating the the logistic difference equation to generate a periodic sequence of decrypting iterates whose values are within a selected range.

24. The method of Claim 22 wherein the logistic difference equation comprises the equation $x_{n+1} = \mu x_n(1 - x_n)$, where μ is a constant and x is an iterated result.
25. The method of Claim 22 wherein the step of iterating the logistic difference equation further comprises
5 the steps of:
 summing the encrypted data with the periodic sequence of decrypting iterates in binary form to generate a second set of decrypting iterates;
 delaying the second set of decrypting iterates for a selected time period; and
 summing the delayed second set of decrypting iterates with encrypted data to be decrypted to
10 generate decrypted data.
26. The method of Claim 22 further comprising the steps of:
 iterating the logistic difference equation and performing the domain transformation a selected
 number of times; and
15 then summing the decrypted iterates with encrypted data to generate decrypted data.
27. A cryptographic system comprising:
 a random number generator;
 a memory for storing one or more cryptographic keys;
20 an arithmetic logic unit and controller means coupled to the random number generator and memory for iterating a predetermined chaotic equation using random numbers generated by the random number generator and the cryptographic key, and for generating a periodic sequence of iterates, and for performing a domain transformation by converting the periodic sequence of iterates into binary form;
 adder means coupled to the arithmetic logic unit and controller means for summing the iterates
25 with digital data; and
 controller means for controlling the operation of and transfer of data between the random number generator, the memory, the arithmetic logic unit and controller means, and the adder.
28. The system of Claim 27 wherein the arithmetic logic unit and controller means iterates a chaotic
30 equation comprising the logistic difference equation $x_{n+1} = \mu x_n(1 - x_n)$, where μ is a constant and x is an iterated result.
29. The system of Claim 27 wherein the arithmetic logic unit and controller means comprises:
 means for adjusting the mathematical precision of the arithmetic logic unit to adjust the periodic
35 sequence of encrypting iterates.
30. The system of Claim 27 wherein the arithmetic logic unit and controller means comprises:
 means for iterating the chaotic equation using a discontinuous set of encrypting iterates.
- 40 31. The system of Claim 27 wherein the arithmetic logic unit and controller means comprises:
 means for periodically perturbing the iterates to add a further discontinuity in the binary encrypting iterates generated by the domain transformation step.
32. The system of Claim 27 wherein the arithmetic logic unit and controller means comprises:
45 means for feeding back the encrypted data;
 means for summing the encrypted data with the periodic sequence of encrypting iterates to generate a second set of encrypting iterates;
 means for delaying the summed second set of encrypting iterates for a selected time period; and
 means for summing the delayed second set of encrypting iterates with digital data to be encrypted
50 to generate encrypted data.
33. The system of Claim 27 wherein the arithmetic logic unit and controller means comprises:
 means for iterating the chaotic equation and performing the domain transformation a selected
 number of times; and
55 means for summing the encrypting iterates with digital data to be encrypted to generate encrypted data.



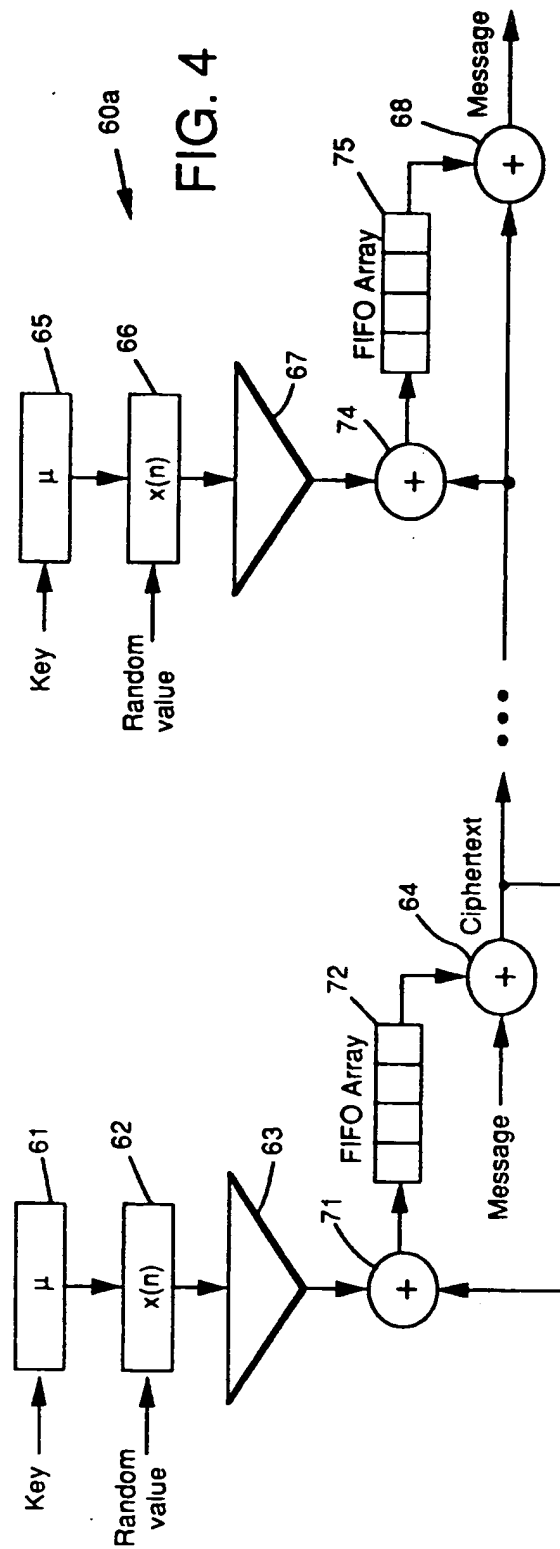
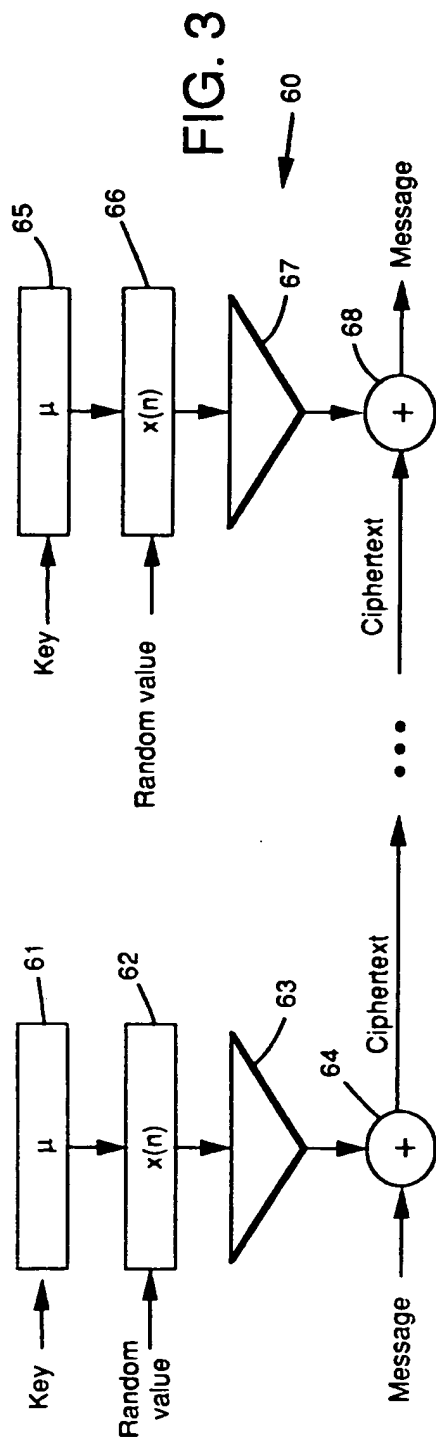


FIG. 5

